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$\alpha$ -shape

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$\alpha$ -shape

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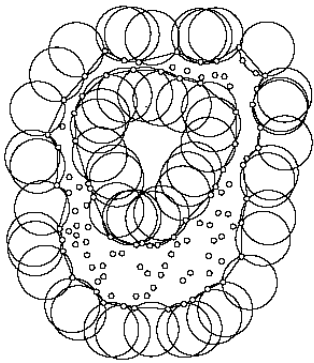
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$\gamma$ -graph

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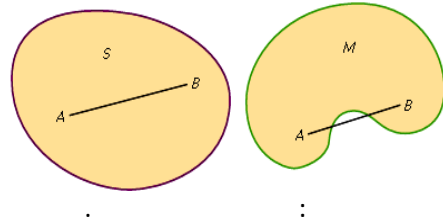
$\alpha$ -shape

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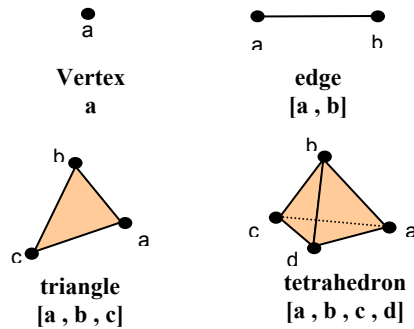
$b \cap S = \emptyset$   
 $\alpha$ -exposed  $k$ -simplex :  $\alpha$ -exposed  
 $b$   $\lambda$ -ball  
 $k$ -simplex  $S$   $b$   
 $b$   $[\ ]$   
 $( )$



$\alpha$ -  
 $1$ -simplex  
 $\alpha$ -exposed  
 $\alpha$ -exposed  $1$ -simplex :  
 $\alpha$ -exposed  $1$ -simplex :  
 $\alpha$ -exposed  $1$ -simplex :  
 $\alpha$ -exposed  $1$ -simplex :  
 $\alpha$ -exposed  $1$ -simplex :  
 $\alpha$ -exposed  $1$ -simplex :

$K+1$  :  $k$ -simplex  
 $K$   $k$ -simplex  $K$   
 $( )$   $( )$   
 $k$ -simplex  $)$

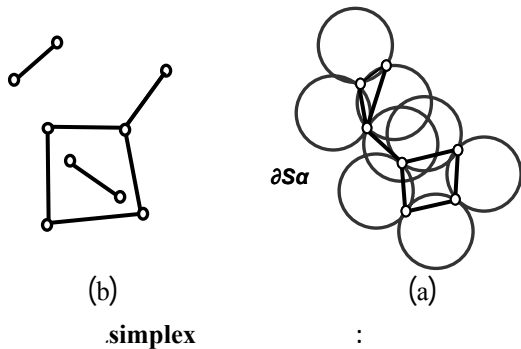
$\alpha$ -  
 $R^d$   $S$  :  
 $0 \leq k < d$   $S$   $k$ -simplex shape  
 $S$   $\alpha$ -exposed  $k$ -simplex



$\partial S_\alpha$   
 $\partial S_\alpha = \{ \Delta T \mid T \in S, |T| \leq d \text{ and } \Delta T \text{ } \alpha\text{-exposed} \}$   
 $( )$   
 $\partial S_\alpha$

$R^d$   $S$  :  
 $) S$   $S$   
 $S$   $($   
 $S$  :  
 $R^3$   
 $[\ ]$

simplex (a)  
 simplex (b)  
 simplex

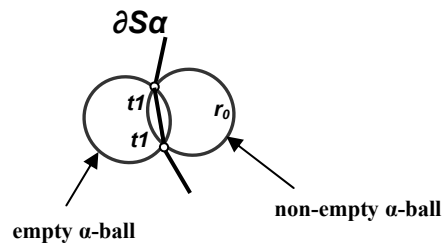
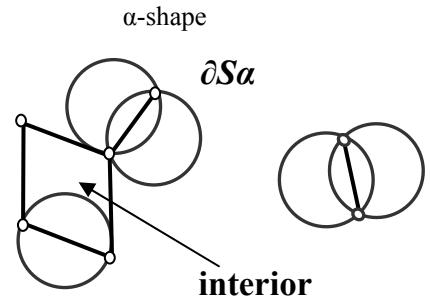


$\alpha$ -shape  
 $\alpha$   
 $\alpha$   
 $b$   $\lambda$ -ball

$k$ -simplex  
 $\Delta T$   $T$   
 $0 < \lambda < \infty$   $\lambda$  :  $\lambda$ -ball  
 $\infty$ -ball  $0$ -ball  $\lambda$ -ball  
 $b$   $\lambda$ -ball



	[ ]	$\Delta T \in \partial C\alpha(S)$	$\Delta T$	:
				$\Delta T \in \partial S\alpha(S)$
<b><math>\alpha</math>-shape</b>		$\partial C\alpha(S) \in \partial S\alpha(S)$	:	
		$\alpha$ -shape	$\alpha$ -Complex	
			:	$\alpha$ -shape
$\alpha$ -	:			
	shape			
DT	$\Delta T$ simplex	:	$C\alpha$	
$\mu T$	$\sigma T$ -ball	.		
	$\Delta T$	$\sigma T < \alpha$		
$\alpha$ -test	)	$C\alpha$		
		(.		
d-	: $C\alpha$	$\alpha$ -shape		
	$S\alpha$	$C\alpha$ simplex		
		$S\alpha$	$C\alpha$	
		( .		
$\sigma T$ -	$\alpha$ -test	( .		
P			ball	
	( .	T	S	
simplex				
		$\Delta T$	$C\alpha$	
simplex				
	S			
	:			
$C\alpha(S)$ simplex	$\Delta T$	:		( )
$C\alpha(S)$	$\Delta T \in \partial Conv(S)$			
$C\alpha(S)$				
$\Delta T$	DT(S) simplex			
	$C\alpha(S)$			
	$\Delta T$ k-simplex			
	$\alpha$			
$C\alpha(S)$	$C\alpha(S)$ simplex			
	$C\alpha(S)$			
	:			
$\Delta T$ is	$\begin{cases} \text{not in } C\alpha & (\text{for } \alpha < a) \\ \text{in } \partial C\alpha & (\text{for } \alpha \in (a, b)) \\ \text{interior to } C\alpha & (\text{for } \alpha \in (b, \infty)) \end{cases}$			



$\alpha$ -shape  $\Delta T$   $\alpha$ -ball  $\alpha$ -Complex  $\alpha$

$\alpha_1 \leq \alpha_2$  :

$S\alpha_1(S) \subset S\alpha_2(S)$   $C\alpha_1(S) \subset C\alpha_2(S)$

$\alpha$ -shape  $C\alpha(S)$

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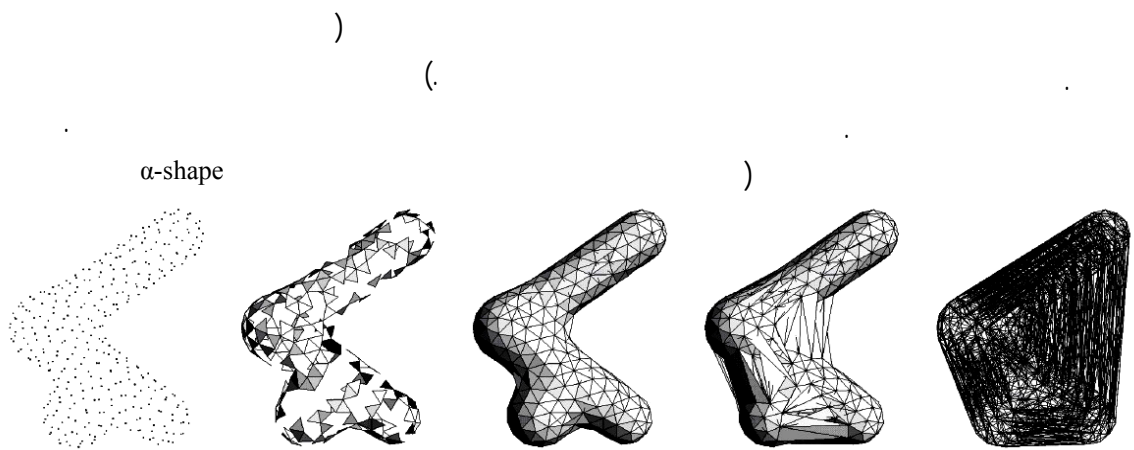
	$\alpha$	$\alpha$
)	$\alpha$	$\alpha \in I = [a, \infty]$
$\alpha$	(	$\Delta T \in S\alpha$
$\alpha$	-	simplex
.	.	simplex
.	.	$\alpha$ -shape
.	.	simplex
-	.	d-simplex
$\alpha$	.	$\sigma T < \alpha$
.	.	d-simplex
.	.	( $\alpha$ -test )
.	.	Complex
.	.	simplex
.	.	d-simplex
.	.	k-simplex
.	.	b a
.	.	k < d
.	.	(k+1)-simplex
.	.	(k+1)-simplex
.	.	$\Delta T$
.	.	k-simplex
.	.	$\Delta T$
.	.	$\Delta V \Delta U$
.	.	simplex super $\Delta V \Delta U$
.	.	$\Delta T$
.	.	:
.	.	:
.	.	DT(S) k-simplex $\Delta T$
.	.	(k+1)- Bu
.	.	k < d
.	.	DT(S) $\Delta U$ simplex
.	.	$\Delta U \in C\alpha$
.	.	a = min {au   Bu = (au, bu), $\Delta U$ (k+1)-
.	.	Simplex $T \subset U$ }
.	.	$\alpha \in (a, \infty)$ $\Delta T \in C\alpha$
.	.	Ca k-simplex $\Delta T$ :
.	.	(k+1)- Bu
.	.	k < d
.	.	DT(S) $\Delta U$ simplex
.	.	$\Delta U \in C\alpha$
.	.	b = max {au   Bu = (au, bu), $\Delta U$ (k+1)-Simplex
.	.	, $T \subset U$ }
.	.	$\alpha \in (b, \infty)$ $\Delta T \in \partial C\alpha$
.	.	$\alpha$ -shape
.	.	$\alpha$ -test
.	.	:
.	.	( )
.	.	:
.	.	( - )
.	.	:
.	.	$\alpha$ -shape

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$\alpha$ -shape

$\alpha$ -shape  
 $\alpha$ -  
 $\alpha$ -ball  
shape  
DTM



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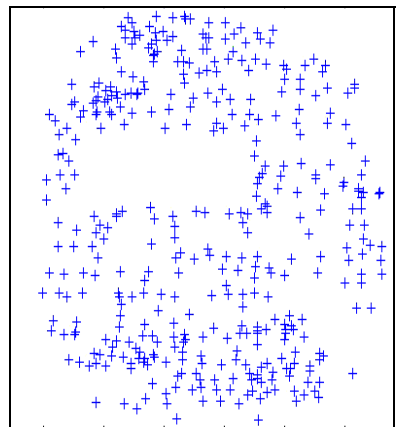
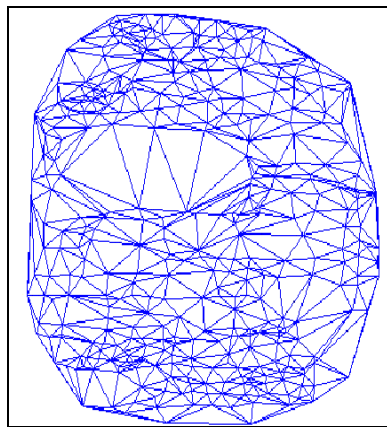
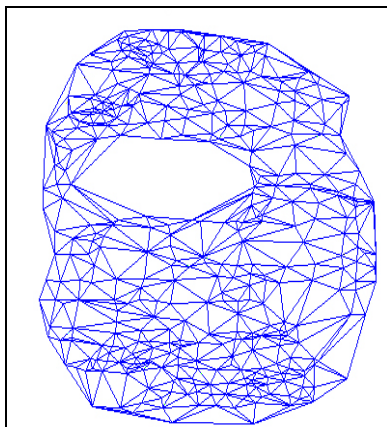
$\alpha$ -shape .

$\alpha$ -shape

$\alpha$ -shape

DTM

$\alpha$ -shape



$\alpha =$   $\alpha$ -shape

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- 1 - DTM =Digital Terrain Model
  - 2 - TIN = Triangles Irregular Networks
  - 3 - ex-Hull
  - 4 - Boissennat
  - 5 - Veltkamp
  - 6 - Hoppe
  - 7 - Zero-Countour
  - 8 - Edelsbrunner
  - 9 - Bernardini
  - 10 - Conexity
  - 11 - Concave
  - 12 - General Position
  - 13 - Boundary
  - 14 - Tiechmann
  - 15 - Capps
-